Digital Communication I: Modulation and Coding Course

Spring - 2015 Jeffrey N. Denenberg Lecture 3: Baseband Demodulation/Detection

Last time we talked about:

- Transforming the information source to a form compatible with a digital system
 - Sampling/Reconstruction
 - Aliasing
 - Quantization
 - Uniform and non-uniform
 - Baseband modulation
 - Binary pulse modulation
 - M-ary pulse modulation
 - M-PAM (M-ary Pulse amplitude modulation)

Formatting and transmission of baseband signal





Assuming real time transmission and equal energy per transmission data bit for binary-PAM and 4-ary PAM:

• 4-ary: $T=2T_b$ and Binary: $T=T_b$

$$A^2 = 10B^2$$



Example of M-ary PAM ...



$$R_{b} = 1/T_{b} = 3/T_{s}$$

R=1/T=1/T_{b} = 3/T_{s}

$$7T_{b} = 3/T_{s}$$

 $T = 1/2T_{b} = 3/2T_{s} = 1.5/T_{s}$

Today we are going to talk about:

- Receiver structure
 - Demodulation (and sampling)
 - Detection
- First step for designing the receiver
 - Matched filter receiver
 - Correlator receiver

Demodulation and detection



Major sources of errors:

- Thermal noise (AWGN)
 - disturbs the signal in an additive fashion (Additive)
 - has flat spectral density for all frequencies of interest (White)
 - is modeled by Gaussian random process (Gaussian Noise)
- Inter-Symbol Interference (ISI)
 - Due to the filtering effect of transmitter, channel and receiver, symbols are "smeared".

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Example: Impact of the channel



Example: Channel impact ...



Receiver tasks

- Demodulation and sampling:
 - Waveform recovery and preparing the received signal for detection:
 - Improving the signal power to the noise power (SNR) using matched filter
 - Reducing ISI using equalizer
 - Sampling the recovered waveform
- Detection:
 - Estimate the transmitted symbol based on the received sample

Receiver structure



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Baseband and bandpass

- Bandpass model of detection process is equivalent to baseband model because:
 - The received bandpass waveform is first transformed to a baseband waveform.
 - Equivalence theorem:
 - Performing bandpass linear signal processing followed by heterodyning the signal to the baseband, yields the same results as heterodyning the bandpass signal to the baseband, followed by a baseband linear signal processing.

Steps in designing the receiver

- Find optimum solution for receiver design with the following goals:
 - 1. Maximize SNR
 - 2. Minimize ISI
- Steps in design:
 - Model the received signal
 - Find separate solutions for each of the goals.
- First, we focus on designing a receiver which maximizes the SNR.

Design the receiver filter to maximize the SNR

Model the received signal



$$r(t) = s_i(t) * h_c(t) + n(t)$$

- Simplify the model:
 - Received signal in AWGN



Matched filter receiver

Problem:

- Design the receiver filter h(t) such that the SNR is maximized at the sampling time when s(t) i=1. A
- Solution:

The optimum filter, is the Matched filter, given by

$$h(t) = h_{opt}(t) = s_i^* (T - t)$$

$$H(f) = H_{opt}(f) = S_i^* (f) \exp(-j2\pi fT)$$



Example of matched filter



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Properties of the matched filter

The Fourier transform of a matched filter output with the matched signal as input is, except for a time delay factor, proportional to the <u>ESD</u> of the input signal.

$$Z(f) = |S(f)|^2 \exp(-j2\pi fT)$$

The output signal of a matched filter is proportional to a shifted version of the autocorrelation function of the input signal to which the filter is matched.

$$z(t) = R_s(t - T) \Longrightarrow z(T) = R_s(0) = E_s$$

The output SNR of a matched filter depends only on the ratio of the signal energy to the PSD of the white noise at <u>the filter input</u>.

$$\max\left(\frac{S}{N}\right)_T = \frac{E_s}{N_0/2}$$

Two matching conditions in the matched-filtering operation: spectral phase matching that gives the desired output peak at time *T*. spectral amplitude matching that gives optimum SNR to the peak value.

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Correlator receiver

The matched filter output at the <u>sampling time</u>, can be realized as the correlator output.

$$z(T) = h_{opt}(T) * r(T)$$

= $\int_{0}^{T} r(\tau) s_{i}^{*}(\tau) d\tau = \langle r(t), s(t) \rangle$

Implementation of matched filter receiver



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Implementation of correlator receiver



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Implementation example of matched filter receivers



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