

14.36 Find $v_o(t)$, for $t > 0$, in the network in Fig. P14.36.

PSV

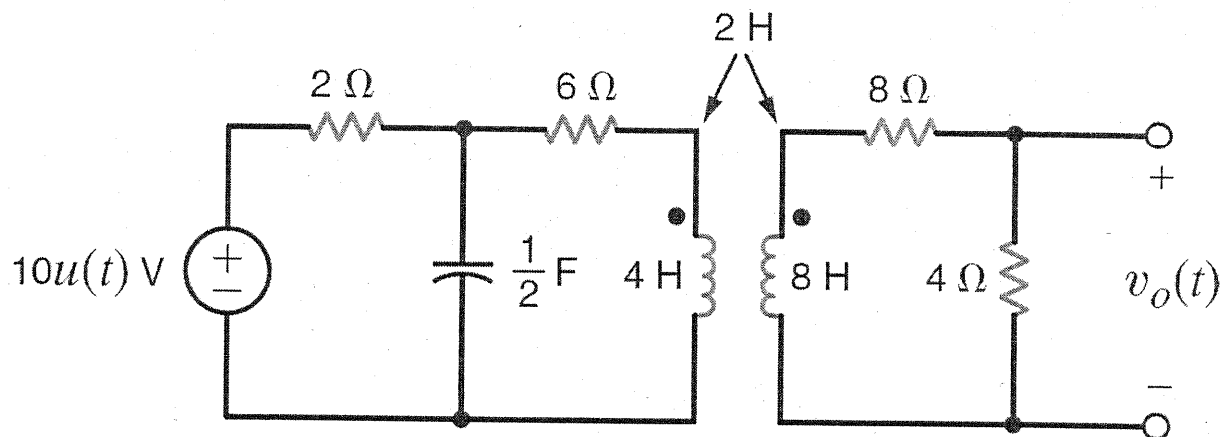
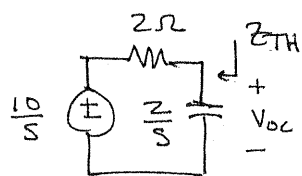


Figure P14.36

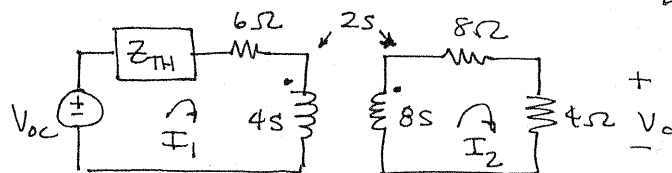
SOLUTION: $t=0^-$: no excitation \Rightarrow ϕ initial conditions

$t=0^+$ (use Thevenin 1st)



$$V_{OC} = \frac{10}{s} \left[\frac{2/s}{2/s + 2} \right] = \frac{10}{s(s+1)} \text{ V}$$

$$Z_{TH} = 2(2/s) / \left[2 + 2/s \right] = \frac{2}{s+1} \Omega$$



$$V_{OC} = I_1(4s + 6 + Z_{TH}) - 2sI_2$$

$$0 = -2sI_1 + I_2(8s + 12)$$

yields, $I_1 = I_2(4s + 6)/s \Rightarrow V_{OC} = I_2 \left[(4s + 6 + Z_{TH})(4s + 6) - 2s \right]$

solve for I_2 and use $V_o = 4I_2$

$$V_o = \frac{20/7}{s^3 + \left(\frac{31}{7}\right)s^2 + \left(\frac{46}{7}\right)s + \frac{24}{7}}$$

Using the ROOTS function in MATLAB yields

$$V_0 = \frac{20/7}{(s+2)(s+1.21-j0.5)(s+1.21+j0.5)} = \frac{A}{s+2} + \frac{K}{s+1.21-j/2} + \frac{K^*}{s+1.21+j/2}$$

$$A = 3.33$$

$$K = 3.15 \angle -122$$

$$v_0(t) = [3.33e^{-2t} + 6.30e^{-1.21t} \cos(t/2 - 122^\circ)] u(t) \checkmark \checkmark$$